Polyurethane microcellular elastomers: 1. Effect of chemical composition on tensile strength and elongation at break of poly(ethylene-butylene adipate) based systems

T. Korodi and N. Marcu

Intreprinderea de Spume Poliuretanice, R-1900 *Timisoara, Celea Buziasului Nr.* 40, *R.S. Romania (Received* 29 *September* 1982; *revised* 20 *January* 1983)

The relationships between tensile strength and elongation at break and the chemical composition of a microcellular elastomer used in shoe sole technology have been calculated using multiple linear regression analysis. Using the statistical Student's test, the importance of the factors that influence the above characteristics have been established. It has been found that the moulded density has the major influence on the tensile strength while the elongation at break depends to a great extent on the hardsegment dispersion into the soft matrix, as indicated by the influence of the water contents and the quasi-prepolymer index (I_{NCO}) . Hydroxyl number in the usual range of 52-61 mg KOH/g has no influence on the above characteristics.

Keyworda Polyurethane elastomer; microcellular polyurethane; shoe sole material; multiple linear regression; polyurethane mechanical properties; liquid reaction moulding polyurethane

INTRODUCTION

Microcellular polyurethanes for shoe soles are of both the polyester and polyether types. Polyester systems are usually based on quasi-prepolymers (obtained from *p,p'* diphenylmethane diisocyanate (MDI) and polyester in the molar ratio of 10-13 : 1), polyester, chain extender (diol or diamine), catalyst, surfactants and water to produce $CO₂$ **--** the blowing agent.

These materials are block copolymers, consisting of alternating blocks of flexible chains (soft segments) and highly polar, relatively rigid blocks (hard segments). The soft segment is the aliphatic polyester, while the hard segment is formed in the reaction of the quasiprepolymer's free MDI and chain extender. Because of the incompatibility of hard and soft segments, the material often undergoes microphase separation, clustering into hard and soft domains. Many studies¹⁻⁶ have been performed to analyse the nature of domain structures and the factors that influence this morphology. Delides and Pethrick⁷, using ultrasonic and dielectric studies, have shown the presence of an 'interfacial' domain between the soft segments and the ordered hard segments.

The presence of crosslinks when the phases are in a mixed state at elevated temperature hinders complete phase segregation at lower temperature, which has an important influence on the material's room-temperature properties⁸.

Polyurethane systems using $CO₂$ as blowing agent assume the existence of crosslinks and/or branches formed by biuret and/or allophanate linkages⁹.

In this study, we propose to find the factors influencing the tensile strength and elongation at break of the polyurethane microcellular elastomer systems used in shoe sole technology, and their importance, by multivariable linear regression analysis.

EXPERIMENTAL

The materials used in this study were a linear polyester, poly(ethylenc-butylene adipate) (PEBA) with hydroxyl number in the range 52-61 mg KOH/g, PEBA and MDI based quasi-prepolymer (free NCO 19.1%), 1,4-butanediol (BASF) and 1,4-diazabicyclo[2.2.2]octane (DA-BCO) (Houdry-Hiils). The concentration ranges of the reagents are presented in *Table 1.*

The polyol blend (PEBA, 1,4-butanediol, DABCO and water) and quasi-prepolymer have been processed on a two-component metering system with mixing characteristics of 3000 rpm and 2.3 kW, output 50 g s^{-1} , using liquid reaction moulding.

Tensile strength and elongation at break have been measured according to ASTM D 638, on samples cut from plates of $300 \times 100 \times 8$ mm, obtained by pouring into a 40°C mould with the above-mentioned metering system. The free rise density has been measured by pouring into a 600 cm^3 open cup. The free rise hardness has been checked on the upper, freely risen, surface of the foam in that cup.

THE MATHEMATICAL MODEL

We suppose that the tensile strength and elongation at break, which we shall call the dependent known variables (P), depend on the chemical composition (x_k) and cellular

character (y_i) of the microcellular elastomer, as known variables or variates. Thus we can write:

$$
f(P) = A_0 + \sum A_k f(x_k) + \sum A_i f(y_{i-q})
$$
 (1)

$$
k=1,2,3,\ldots,q; i=q+1,q+2,q+3,\ldots,m
$$

where f represents the linear, reciprocal, logarithmic and minus logarithmic transformations of the dependent known variables (P) and variates (x_k, y_{i-q}) ; x_k is the kth chemical constituent and x is its concentration; and y_{i-q} is the $(i-q)$ th parameter concerning the cellular structure of the material and y is its value.

The regression coefficients A_k and A_i become the unknown parameters that can be statistically determined, by using the principle of least squares¹⁰, which leads to the system of equations:

KQ=M

where

$$
\mathbf{K} = \begin{bmatrix} n \sum f(x_1) \sum f(x_2) \cdots \sum f(y_1) \cdots \sum f(y_{m-q}) \cdots \\ \sum f(x_1) \sum f(x_1) \sum f(x_2) \cdots \sum f(x_1) \sum f(y_1) \cdots \sum f(x_1) \sum f(y_{m-q}) \cdots \\ \vdots \\ \sum f(y_1) \sum f(y_{m-q}) \sum f(y
$$

symmetric

$$
\sum f(y_{m-q})_j^2
$$
\n
$$
\mathbf{Q} = \begin{bmatrix} A_0 \\ A_1 \\ A_2 \\ \vdots \\ A_{q+1} \\ \vdots \\ A_m \end{bmatrix} \quad \mathbf{M} = \begin{bmatrix} \sum^r (P)_j \\ \sum f(x_1)_j f(P)_j \\ \sum f(x_2)_j f(P)_j \\ \vdots \\ \sum f(y_1)_j f(P)_j \\ \vdots \\ \sum f(y_{m-q})_j f(P)_j \end{bmatrix}
$$

where $j = 1, 2, 3, ..., n$.

In every case the symbol Σ indicates summation over all the n measurements according to the chemical composition. The statistical parameters established to estimate the relation are:

(1) The multiple correlation coefficient R , which is a measure of the significance of the linear relationship between the variate functions, $f(x_k)$ and $f(y_{i-q})$, and the dependent known variable function, $f(P)$:

$$
R^{2} = 1 - \frac{S}{\sum f(P)_{j}^{2} - (\sum f(P)_{j})^{2}/n}
$$
 (2)

where

$$
S = \sum [f(P)_j - f(\hat{P})_i]^2
$$

S is the sum of squared errors or deviations between measured $f(P)$ and calculated $f(\hat{P})$ quantities, over all the n measurements. The equations characterized by $R² \le 0.4$ represent no relationship between the variates x_k and y_{i-a} and variable P^{11}

(2) The Fisher statistics F , in order to test the significance of the multiple correlation coefficient:

$$
F = \frac{n-m-2}{m+1} \times \frac{R^2}{1-R^2}
$$
 (3)

In this case F signifies the F-distribution with $n-m-2$ and $m+1$ degrees of freedom. The quality of the relationship depends on the significance level of $F¹²$

(3) The significance level of the regression coefficients A_k and A_i has been estimated by the Student's t statistic:

$$
t = \frac{A_{k(i)}}{\sigma \sqrt{d_{ee}}} \tag{4}
$$

in which d_{ee} are the diagonal elements of the K^{-1} matrix, while $\sigma^2 = S/(n-m-2)$. A significance level lower than 90% associated with the regression coefficient $A_{k(i)}$ through the t parameter indicates no influence of the variates x_k or y_{i-q} on the variable P, and thus it can be neglected.

RESULTS AND DISCUSSION

The variation of tensile strength (7S) and elongation at break *(EB)* depending on the chemical composition (x_k) and foam properties (y_{i-q}) are summarized in *Table 2*. The correlation of $T S$ or $E B$ with only one parameter x_k (Table 3) leads to a meaningless relationship. The R and F values obtained are presented in *Table 4,* taking into consideration all the parameters x_k . In the case of TS there is also a meaningless relationship, while in the case of *EB a* poor correlation is obtained, These results suggest that the cellular character influences these characteristics as well. In this context the y_{i-a} parameters have been introduced *(Table 2)* as a potential characterization of the cellular structure. The correlations carried out with the parameters y_{i-q} lead to similar statistical results as in the case of the parameters x_k (Tables 5 and 6).

We can therefore state that both tensile strength and elongation at break depend on the chemical composition of the polymer and it's cellular structure. The regression coefficients A_k and A_i and the statistical parameters of the correlational analysis are presented in *Tables 7* and 8. In both cases, the largest values of R and F indicate that the best fit is obtained for a linear function of the parameters:

$$
f(P) = P
$$
; $f(x_k) = x_k$; $f(y_{i-q}) = y_{i-q}$

Considering the significance level of the statistical Student's t test, it can be observed that the tensile strength does not depend on the free rise hardness (y_2) , free rise density (y_3) or the OH number of the polyester (x_4) .

 x_1 = parts by weight water

 x_2 = parts by weight 1,4-butanediol

 x_3 = quasi-prepolymer index

 x_4 = PEBA hydroxyl number (mg KOH/g)

 y_1 = moulded density (g cm⁻³)

 y_2 = free rise hardness (\degree Sh A)

 y_3 = free rise density (g cm^{-3})

Similarly, the elongation at break is not influenced by the free rise density (y_3) , the 1,4-butanediol contents (x_2) or the OH number of the polyester (x_4) .

The correlation parameters obtained by neglecting the above parameters are summarized in *Tables 9* and *I0.* Again, the best fit is obtained in the case of a linear function of the parameters. The increase in magnitude of F shows an enlargement of the significance of the relation obtained.

The importance of the influencing factors is estimated by the increasing order of the $t_{k(i)}$ magnitudes. Thus, tensile strength depends to the largest extent on the moulded density, the water contents having the least influence, whereas it has the largest influence on the elongation at break.

Table 4 Correlational data of *TS* and *EB* considering all the parameters *x k*

An increase of the water concentration and the quasiprepolymer index leads to a decrease of the elongation at break. A higher content of water and isocyanate assumes the setting-up of more NH groups liable to build up

Polyurethane microcellular elastomers: 1: T. Korodi and N. Marcu

Table 5 Correlation coefficients ($R²$) obtained by the correlation of TS or *EB* with the parameters y_{i-q}

hydrogen bonding and/or chemical crosslinks by allophanate and/or biuret, which leads to impairment of the ability of the material to reach complete phase separation at room temperature^{8,13,14}, referring to the mixed state of **the domains at the reaction temperature (140°-150°C). The dispersed hard blocks in the soft-segment matrix**

Table 6 **Correlational data of** *TS* **end** *EB* **considering all the parameters** *Yi--q*

	TS		EВ	
	R	F	R	F
Linear	0.671	5.5	0.759	9.2
Reciprocal	0.611	4.0	0.725	7.5
Logarithmic Minus	0.663	5.3	0.750	8.7
logarithmic	0.661	5.2	0.749	8.6

reduce the latter's mobility, lowering the active elongation space, which finally leads to the decrease of the elongation at break.

It is difficult to attribute physical meaning to the free rise hardness, but considering the formation mechanism of these systems¹⁵, as well as the higher reaction rate of addition rather than of CO₂ formation¹, the assumption **that it depends on the cellular structure formed during the reactions is plausible. The increase of the elongation at break with the moulded density and free rise hardness shows an important influence of the cellular structure on this property.**

The independence of the elongation at break from the relatively small variation of the hard-segment content, expressed as the negligible influence of 1,4-butanediol, suggests the major role of the soft domains in this phenomenon. The same results were obtained in the case of a polyether based polyurethane¹⁷ in the range of **30-40% hard-segment content.**

Table 7 **Results of the correlational analysis of the tensile strength** *(TS) (k* **and i according to equation** (1) with q = 4)

Polyurethane microcellular elastomers: 1: T. Korodi and N. Marcu

Table 8 Results of the correlational analysis of the elongation at break *(EB) (k* and i according to equation (1) with q = 4)

Table 9 Correlational data of the tensile strength *(TS)* considering the significant parameters (k and *i* according to equation (1) with $q = 4$)

Table 10 Correlational data of the elongation at break *(EB)* considering the significant parameters (k and i according to equation (1) with $q = 4$

The most important factor that influences the tensile strength is the moulded density, as expected according to the fracture mechanism¹⁸.

The hard-segment concentration has a positive effect on the tensile strength observed by its increasing with the 1,4-butanediol and isocyanate contents, which is in agreement with the widely accepted idea that the rigid domains reinforce the elastomeric matrix by functioning as filler particles $19,20$.

The presence of water in the system leads to the formation of urea type hard segments, which form quasiamorphous domains²¹. Polyurethaneureas exhibit a mixing of hard segments into the soft matrix 22 . Thus, the reducing effect of the water content is due to the decrease of the hard domain crystallinity as well as its dispersion into the soft matrix, which produces stress concentrations in these points, leading to critical fracture regions.

Variation within the usual range of hydroxyl number (50-60 mg KOH/g) influences neither the tensile strength nor elongation at break.

CONCLUSIONS

The important influence of hard-segment dispersion into the soft matrix on the elongation at break, observed by its dependence on the water and isocyanate contents, its independence from the variation of the hard-segment content, as well as the significant effect of the cellular structure, allows us to suppose that this phenomenon is essentially due to the elongation and orientation of the soft segment and cellular system in the stretch direction.

The tensile strength depends to the greatest extent on the moulded density. An important positive effect of the hard-segment content can also be noted. The water content has a less important influence compared to its effect on the elongation at break.

The hydroxyl number of the polyester, in the limits of 52-61 mg KOH/g, has no influence on the properties studied, which is useful information for the industrial

application of this material.

REFERENCES

- 1 McBride, J. S., Massaro, T. A. and Cooper, *S. L. J. Appl. Polym. Sci.* 1979, 23, 201
- 2 Hesketh, T. R., Van Bogart, J. W. C. and Cooper, S. L. *Polym.* Eng. Sci. 1980, 20 (3), 190
- 3 Srichatrapimuk. V. W. and Cooper, *S. L.J. Macromol. Sci.-Phys.* B 1978, 15 (2), 267
- 4 Lilianitkul, A. and Cooper, S. L., 'Advances in Urethane Science and Technology' (Eds. K. C. Frisch and S. L. Reegen), vol. 7, Technomic, 1979, p. 163
- 5 Estes, G. M., Seymour, R. W., Huh, D. S. and Cooper, S. L. *Polym. Eng. Sci.* 1969, 9 (6), 383
- 6 Huh, D. S. and Cooper, S. L. *Polym. Eng. ScL* 1971, 11 (5), 369
- 7 Delides, C. and Pethrick, R. A. *Eur. Polym. J.* 1981, 17, 675
8 Assink, R. A. and Wilkes, G. L. *J. Annl. Polym. Sci.* 1981, 26, 36
- *8 Assink, R.A. andWilkes, G.L.J.AppI. Polym. Sci. 1981,26,3689*
- 9 Saunders, J. H. and Frisch, K. C., 'Polyurethanes Chemistry and Technology', part I, 'Chemistry', Interscience New York, 1965, p. 220
- 10 Kendall, M. and Stuart, A., 'The Advanced Theory of Statistics', Griffin, London, 1979
- 11 Topliss, J. R. and Costello, *R. J. J. Med. Chem.* 1972, 15, 1066
- 12 Charton, M. and Charton, B. I. J. Org. Chem. 1973, 38, 1631
13 Cooper. S. L., West. J. C. and Seymour, R. W. 'Encyclopedia
- Cooper, S. L., West, J. C. and Seymour, R. W., 'Encyclopedia of Polymer Science and Technology', Supplement No. 1, John Wiley, New York, 1976, p. 541
- 14 Redman, R. P., 'Developments in Polyurethane 1' (Ed. J. M. Buist), Applied Science, London, 1981, p. 34
- 15 Lipatova, T. E. *Hsokomol. Soedin Ser. A* 1973, 15 (2), 327
- Saunders, J. H. and Frisch, K. C., 'Polyurethanes Chemistry and Technology', part I, 'Chemistry', Interscience, New York, 1965, p. 129
- 17 Zdrahala, R. J., Critchfield, F. E., Gerkin, R. M. and Hager, S. L. *J. Elast. Plast.* 1980, 12, 184
- 18 Manson, J. A. and Sperling, L. H., 'Polymer Blends and Composites', Heyden, London and New York, 1976, p. 32
- 19 Ng, H. N., Allegrezza, A. E., Seymour, R. W. and Cooper, S. U *Polymer* 1973, 14, 255
- 20 Foks, J., Janik, H. and Winiecki, *S. J. Appl. Polym. ScL* 1982, 27, 645
- 21 Cambcrlin, Y., Pascault, J. P., Letoffe, M. and Claudy, P. J. *Polym. ScL, Polym. Chem. Edn.* 1982, 20, 1445
- 22 Hu, C. B., Ward, R. S. Jr. and Schneider, *N. S. J. Appl. Polym. Sci.* 1982, 27, 2167